

Chapter 8.5: Add and Subtract Rational Expressions

How do you add fractions?

need a common denominator
LCM

How do you subtract fractions?

same as add.

$$\frac{1}{3} - \frac{2}{5} = \frac{5}{15} - \frac{6}{15} = \frac{-1}{15}$$

$$\frac{7}{4x} + \frac{3}{4x}$$

$$\frac{10}{4x}$$

$$\boxed{\frac{5}{2x}}$$

$$\frac{2x}{x+6} - \frac{5}{x+6}$$

$$\boxed{\frac{2x-5}{x+6}}$$

Find the LCM

$$4x^2 - 16$$

$$6x^2 - 24x + 24$$

$$4(x^2 - 4)$$

$$6(x^2 - 4x + 4)$$

$$4(x+2)(x-2)$$

$$6(x-2)(x-2)$$

$$2(2)(x-2)(x+2)$$

$$2(3)(x-2)(x-2)$$

$$2(2)(3)(x-2)(x+2)(x-2)$$

$$\frac{7(x+1)}{9x^2} + \frac{x}{3x^2 + 3x}$$

$3(3)x^2(x+1) \quad 3x(x+1) \quad 3x$

$$\frac{7(x+1) + 3x \cdot x}{(3)(3)x^2(x+1)} = \frac{3x^2 + 7x + 7}{9x^2(x+1)}$$

$$\frac{x+2}{2x-2} - \frac{-2x-1}{x^2-4x+3}$$

$$\frac{x+2}{2(x-1)} - \frac{-1(2x+1)2}{(x-3)(x-1)2}$$

$$\frac{(x+2)(x-3) - [-1(2x+1)(2)]}{2(x-1)(x-3)}$$

$$\frac{x^2 - x - 6 + (+4x + 2)}{2(x-1)(x-3)}$$

$$\frac{x^2 + 3x - 4}{2(x-1)(x-3)} = \frac{(x-1)(x+4)}{2(x-1)(x-3)}$$

$$\boxed{\frac{x+4}{2(x-3)}}$$

Complex Fractions:

Fractions within fractions

simplified by working with the innermost fractions first and working your way out.
GOAL is to have one fraction.

$$\frac{\frac{1}{2}}{\frac{\frac{1}{15}}{\frac{1}{5}} - \frac{\frac{2}{5}}{\frac{6}{15}}}$$

$$\left[\frac{\frac{1}{2}}{\frac{1}{15}} \right] \quad \left[\frac{15}{-2} \right]$$

Let f be the focal length of a thin camera lens, p be the distance between an object being photographed and the lens, and q be the distance between the lens and the film. For the photograph to be in focus, the variables should satisfy the lens equation below.

Simplify the fraction

$$f = \frac{1}{\frac{1}{p} + \frac{1}{q}}$$

$$\begin{aligned} \frac{\frac{5}{x+4}}{\frac{1x}{x(x+4)} + \frac{2(x+4)}{x(x+4)}} &= \frac{\frac{5}{x+4}}{\frac{x+2x+8}{x(x+4)}} = \left[\frac{\frac{5}{x+4}}{\frac{3x+8}{x(x+4)}} \right] \\ &= \frac{\cancel{5x}(\cancel{x+4})}{(\cancel{x+4})(3x+8)} = \boxed{\frac{5x}{3x+8}} \end{aligned}$$

Homework: Chapter 8.5 pg. 586
#'s 4,14,18,20,22,24,26,30,32,36